

How can power-to-ammonia be robust?

Optimization of an ammonia synthesis plant powered by a wind turbine considering operational uncertainties.

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Abstract

The increasing share of wind energy induces a strain on the electricity network. To unburden the transmission system operators from this strain, the dispensable wind energy can locally be stored in an energy carrier, e.g. ammonia (NH₃). Existing work considers fixed operational parameters during design optimization to represent real-life conditions of the Power-to-Ammonia (PtA) system. However, uncertainties significantly affect real-life performances, which can lead to suboptimal plants. To provide a robust design –least sensitive to uncertainties– we considered the main operational uncertainties during design optimization and illustrated the contribution of each uncertainty on the systems NH₃ production. This work presents the optimization under uncertainty of the PtA process and a global sensitivity

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analysis on the optimal designs. The results revealed a design trade-off, where a *productive* design produces 3.2 times more NH_3 on average but is 2.6 times less robust (higher standard deviation) than the *robust* design. A global sensitivity analysis on the most robust design showed that the temperature fluctuation of the NH_3 reactor dominates the average ammonia production by 99.7%, while the wind speed measurement error and the temperature variation both influence the ammonia production of the most productive design by 75.4% and 22.5%. Accordingly, an accurate anemometer and improving the temperature control over the NH_3 reactor are the most effective actions to make the most productive design more robust. However a robust plant can be obtained by decreasing the load size of the plant, it suffices improving the temperature control over the NH_3 reactor to make this design (adopted from the trade-off) less sensitive to the noise. Future investigations involve analyzing the dynamical operations of the robust PtA pathway and analyze the impact of uncertainties on its levelized cost.

Keywords: Power-to-ammonia, Robust design optimization, Haber-Bosch synthesis, Seasonal hydrogen storage, Energy storage system

1. Introduction

The erratic nature of renewable sources requires a higher degree of flexibility of the electricity grid [1]. To avoid this requirement, an energy storage system is necessary to regulate the supply of this non-dispatchable energy, removing its intermittent effect on the grid. The primary purpose of the storage system is to capture the excess energy at any time and inject it back into the grid to compensate for variability between supply and demand without

8 relying on fossil fuels, improving the security of electricity supply in a sus-
9 tainable way [2, 3]. For significant power levels, the production of chemicals
10 can be employed to store the energy in a electrochemical energy carrier. This
11 energy carrier could subsequently fuel a power production system for power
12 generation; balancing the electricity network for prolonged power disruptions
13 and reduce the need for a flexible grid [4].

14 The hydrogen-based Power-to-Power (PtP) concept enables the storage
15 of large-scale (\sim MW) power via water electrolysis, but realizing it in prac-
16 tice is proven difficult. The interest in environmental concerns increased in
17 recent years, which helped to lower the cost of renewable energy technolo-
18 gies. This economic trend promoted the creation of numerous research and
19 demonstration projects across Europe [5, 6, 7, 8]. However, storing pure H_2
20 in a compressed or cryogenic (below -253°C) container for several months
21 provides low PtP efficiencies (between 34% and 38%) [9]. Besides, the stor-
22 age of this substance initiates safety issues [10, 11]. A more viable and safer
23 way for the implementation of this hydrogen-based energy storage system is
24 by converting the electrolytic H_2 to ammonia (NH_3), using the industrially
25 mature Haber-Bosch Synthesis (HBS) process [12]. The HBS process con-
26 sists of synthesizing a mixture of H_2 and nitrogen gas (N_2) to form NH_3 in
27 the presence of a catalyst at an operational temperature between 350°C and
28 550°C and a pressure ranging from 150 bar to 250 bar [13, 14, 15].

29 NH_3 gained a significant role during recent years in the application of
30 large-scale H_2 storage, but also for its potential utilization as a maritime fuel
31 and sustainable nitrogen-based fertilizer [16, 17, 18, 19, 20]. Morgan et al.
32 [13] developed an analytic model to determine in which circumstances this

33 concept of Power-to-Ammonia (PtA) can be economically viable in addition
34 to a diesel-fueled generator for a geographic islanded case. A more exten-
35 sive analysis by Bañares-Alcántara et al. investigated the potential use of
36 the NH_3 -based energy storage in electric islanded cases [14]. Later on, the
37 Institute for Sustainable Process Technology (ISPT) presented a feasibility
38 study for implementing this renewable NH_3 concept of storing the abundance
39 of wind energy for local farming and power generation in the Netherlands by
40 considering economic and industrial competitive scenarios [9]. The presence
41 of uncertainties are however observed by Reese et al. on the operations of a
42 small-scale ammonia synthesis pilot plant located in Minnesota, in the form
43 of temperature and pressure fluctuations in the reactor [17]. Although these
44 studies each included a sensitivity analysis of the operations of the electrolyz-
45 ers and the HBS process, no investigation has been done on the identification
46 and quantification of operational uncertainties influencing the performance
47 of the entire storage system design.

48 This paper provides the modeling of the NH_3 -based energy storage to-
49 gether with the identification of reported operational uncertainties from lit-
50 erature, which was combined to ultimately preform a design optimization un-
51 der uncertainties. We performed consecutively the modeling in Aspen Plus
52 of an electrolyzer operating with an alkaline electrolyte, a Pressure Swing
53 Adsorption (PSA) to obtain nitrogen from air, and a Haber-Bosch Synthe-
54 sis (HBS) plant to synthesize NH_3 . In addition to the chemical modeling
55 in Aspen Plus, a Wind Turbine Generator (WTG) is created in Python to
56 convert wind speed into electric power. These models were assembled and
57 optimized with a Multi-Objective Genetic Algorithm (MOGA) to establish

58 a set of optimal designs. This energy model was then combined with the
59 identified operational uncertainties of each subsystem to establish an opti-
60 mization under uncertainty by the use of an Uncertainty Quantification (UQ)
61 algorithm. With the MOGA and UQ approaches, a set of designs was de-
62 termined which were least sensitive to the effect of these uncertainties while
63 maximizing the NH_3 production. This so-called Robust Design Optimization
64 (RDO) approach robustified the performance of the plant. The RDO pro-
65 cess consisted of combining the Nondominated Sorting Genetic Algorithm
66 (NSGA-II) [21] and the Polynomial Chaos Expansion (PCE) technique [22],
67 which ultimately evolved the defined design parameters towards a better
68 performance while taking into account the implemented uncertainties.

69 **2. Modeling the storage of wind energy through ammonia synthesis**

70 This section presents the design of each process necessary to store wind
71 energy in the energy carrier NH_3 . The first subsection provides the wind
72 speed data used to power the storage system. This power is determined by the
73 model of a wind turbine in Python. Each following subsection presents the
74 modeling of an Alkaline Water Electrolyzer (AWE), a PSA and the HBS in
75 Aspen Plus. The description and integration of the operational uncertainties
76 are included for the wind turbine model, the AWE and the HBS at each
77 corresponding subsection.

78 *2.1. Wind power generation*

79 We incorporated the hourly wind speed measurement data of a wind
80 turbine park located in Galicia (Spain) and sequentially sorted the data in
81 a wind speed frequency distribution with a step size of 1 m/s [23]. Through

82 the integration of a power curve of a typical wind turbine model, this wind
 83 speed data is converted into electric power. We based this power curve on the
 84 design of the Vestas V112 onshore wind turbine and integrated this curve in
 85 Python through Equation 1 to calculate the generated wind power (P_{WTG}):

$$P_{\text{WTG}} = \frac{1}{2}\rho AC_P v^3 \quad [\text{W}], \quad (1)$$

86 where ρ is the density of air in kg/m^3 (at sea level and at 15°C , $\rho = 1.22$
 87 kg/m^3), A is the area of the rotating blades in m^2 , C_P is the power coefficient
 88 and v is the wind speed in m/s .

89 In the adopted model, the maximum power output was adjusted to 3 MW
 90 at a rated wind speed of 11 m/s while assuming a constant power coefficient of
 91 37%. We performed this adaptation to correlate the wind speed and electric
 92 power between the cut-in and rated wind speed with the cubic relationship
 93 (Equation 1) without taking into account the dependency of C_p on the wind
 94 speed. The original and adopted design specification are provided in Table
 95 1.

96 Wind turbines are inherently influenced by a variety of uncertainties,
 97 providing ambiguous prospects for start-up wind turbine parks. These un-
 98 certainties have a direct effect on the profitability of these projects, which are
 99 mainly based on wind speed measurements or estimations to forecast the ca-
 100 pacity factor [26] or the Annual Energy Production (AEP) of a location [27].
 101 Lackner et al. categorized a variety of uncertainties influencing this AEP in
 102 four categories, which consists of: wind speed measurement uncertainty, his-
 103 torical wind speed data, wind resource modeling variability, and lastly, the
 104 site assessment uncertainty [27]. Because the wind speed measurements for

Table 1: Wind turbine generator design specifications, constraints and wind speed measurement uncertainty.

Design specification		Reported value [24]	Adopted value
C_P	[W/W]	$C_P(v)$	37.0
A	[m ²]	9852.0	9852.0
Constraints			
$v_{\text{cut-in}}$	[m/s]	3	3
v_{rated}	[m/s]	12	11
$v_{\text{cut-out}}$	[m/s]	25	25
Uncertainty		Integrated value [25]	
$e_{\text{measurement}}$	[-]	$\pm 1\%$	

105 one year are used in this design optimization study (not the power produc-
 106 tion of an actual wind turbine) only the first category of Lackner et al. (the
 107 wind speed measurement error) is applied to the design of the WTG and
 108 furthermore considered in the UQ analysis. Kaganov et al. designated the
 109 wind speed measurement error of rotational measurement devices between
 110 1% and 6% [25]. We choose to integrate a wind speed uncertainty of 1%
 111 to consider the most accurate wind speed measurement in the wind turbine
 112 design. This uncertainty is characterized by a Gaussian distribution in the
 113 UQ analysis which assess for each design the uncertainty propagation on the
 114 considered objective. The following expression enables the implementation
 115 of this uncertainty (Equation 2):

$$v_{\text{measurement}} = v_{\text{data}}(1 - e_{\text{measurement}}) \quad [\text{m/s}], \quad (2)$$

116 where $v_{\text{measurement}}$ is the measured wind speed in m/s resulted from the input
 117 wind data (v_{data}) and the error of the device ($e_{\text{measurement}}$) in %. During the
 118 robust design process, the measured wind speed ($v_{\text{measurement}}$) replaces the
 119 wind speed (v) in Equation 1.

120 2.2. Alkaline water electrolyzer

121 An Alkaline Water Electrolyzer (AWE) was selected because of its proven
 122 reliability in industrial applications and a multitude of commercially available
 123 technologies on the market, allowing the AWE to operate commercially at
 124 MW scale [15, 28, 29]. The AWE process was modeled in Aspen Plus for
 125 one electrolytic cell (Figure 1). To resemble the real operation of an AWE
 126 and determine the hydrogen production when applying electric power to the
 127 electrolyzer stack, the electrolyzer model of Ulleberg [30] is integrated with
 128 a FORTRAN calculator in the ‘Electrolytic cell’ block (Figure 1). Ullebergs
 129 electrolyzer model consists of two empirical equations: a voltage-current (U -
 130 I) relationship and the characterization of the Faraday efficiency (η_F).

131 The applied voltage U on the electrolytic cell is determined by the re-
 132 versible voltage U_{rev} of the electrolytic reaction, the current I flowing through
 133 the electrolytic cell and T the operational temperature of the electrolytic cell.
 134 This relationship is defined with the following expression [30]:

$$\begin{aligned}
 U_{\text{real}} = U_{\text{rev}} + (r_1 + r_2 T) \frac{I}{A} \\
 + (s_1 + s_2 T + s_3 T^2) \log \left((t_1 + t_2/T + t_3/T^2) \frac{I}{A} + 1 \right) \quad [\text{V}],
 \end{aligned}
 \tag{3}$$

135 where r_i are the parameters related to the ohmic resistance of the electrolyte
 136 (for $i = 1, 2$), s_i and t_i are the coefficients for overvoltage on the electrodes

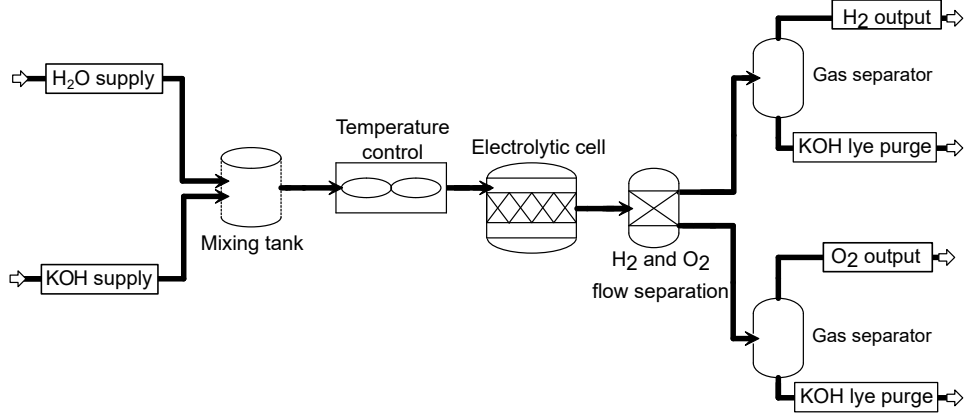


Figure 1: In the Aspen Plus model of the alkaline electrolyzer, KOH lye is dissolved in a tank with water (H_2O), where its exothermic reaction increases the temperature of the mixture. A heat exchanger controls the temperature of the alkaline solution flowing to the electrolytic cell. The block components of one electrolytic cell and the product separation creates the H_2 and O_2 flows. The gas separation blocks separate the H_2 gas and KOH mixture, where the same process occurs on the O_2 production side.

137 (for $i = 1,2,3$) and A the surface area of the electrodes in m^2 . Ulleberg
 138 determined the value of these parameters (r_i , s_i and t_i) by a non-linear
 139 regression deterministic process (see Table A.4) [30].

140 The amount of hydrogen produced by the electrolyzer is determined with
 141 Faraday's law. This law states that the molar flow rate of the produced
 142 hydrogen (\dot{n}_{H_2}) depends on the total number of electrolytic cells N and the
 143 transfer rate of electrons (Equation 4) [30]:

$$\dot{n}_{\text{H}_2} = \eta_{\text{F}} \frac{NI}{zF} \quad [\text{mol/s}], \quad (4)$$

144 where η_{F} is the Faraday efficiency of the electrolytic reaction. This Faraday
 145 efficiency expresses the ratio of the flow rate of hydrogen that is produced

146 by the alkaline electrolyzer, over the theoretical production rate. This ratio
147 is expressed by the second empirical formula with Equation 5 [30]:

$$\eta_F = f_1 \exp\left(\frac{f_2 + f_3 T}{I/A} + \frac{f_4 + f_5 T}{(I/A)^2}\right) \quad [-], \quad (5)$$

148 where f_i (for $i = 1, \dots, 5$) are the parameters defining the evolution of the
149 Faraday efficiency, determined by the same non-linear regression process used
150 in Equation 3 at an operational pressure of 7 bar (Table A.4) [30].

151 Mori et al. studied the steady-state operations of an alkaline electrolyzer,
152 where a sinusoidal behavior of the cell temperature is observed. This tem-
153 perature varied with a range of $\pm 3^\circ\text{C}$ from the desired temperature [31].
154 The study acknowledged that the heat exchanger controlling the tempera-
155 ture causes this variation in temperature. When implementing this variation
156 in the temperature control block of the AWE Aspen Plus model, the Faraday
157 efficiency (Equation 5) and cell current (through the U-I relationship defined
158 with Equation 3) are affected by this uncertainty, resulting in a variance of
159 hydrogen production (Equation 4). This operational uncertainty is therefore
160 included during the global sensitivity analysis and the robust optimization
161 within this study. The UQ analysis assesses the effect of the variation of the
162 cell temperature for each GA-generated design on the investigated output.

163 *2.3. Pressure swing adsorption*

164 The Pressure Swing Adsorption (PSA) process is selected to obtain ni-
165 trogen from the air. Frattini et al. proposed a simplified model of the PSA
166 process in Aspen Plus[®], where the design incorporates a single stage com-
167 pressor, to pressurize the air flow (consisting of 75.5 wt% N₂), and a sepa-
168 ration block, to obtain nitrogen [15]. The same philosophy has been used in

169 Morgan et al. for a mathematical model of a wind-powered ammonia plant
 170 in steady-state operations [13]. The nitrogen production depended in both
 171 cases on the delivered power to the PSA compressor, which can be expressed
 172 with the following relationship between the power P_{PSA} and the air mass flow
 173 rate \dot{m}_{air} [13]:

$$P_{\text{PSA}} = \frac{\dot{m}_{\text{air}}}{\eta_{is}\eta_{\text{mech}}} \left(\frac{k}{k-1} \right) T_{\text{in}} R \left[\left[\frac{p_{\text{out}}}{p_{\text{in}}} \right]^{\frac{(k-1)}{k}} - 1 \right] \quad [\text{W}], \quad (6)$$

174 where η_{is} is the isentropic efficiency ($\eta_{is} = 0.75$ [13]), η_{mech} the mechanical
 175 efficiency ($\eta_{\text{mech}} = 0.95$ [13]), T_{in} the inlet temperature in K, R the gas
 176 constant of air in J/kgK, k the heat capacity ratio ($k = 1.4$), p_{out} the outlet
 177 pressure in bar ($p_{\text{out}} = 7$ bar), and p_{in} the inlet pressure in bar ($p_{\text{in}} = 1$
 178 bar). The mass flow of air (\dot{m}_{air}) is split into a pure mass flow nitrogen
 179 and a residual flow of O₂ and Ar by a separation block in Aspen Plus[®].
 180 The compressor and separator block in Aspen Plus[®] uses the PENG-ROB
 181 property method, which is based on the Peng-Robinson cubic equation of
 182 state [15].

183 2.4. Haber-Bosch synthesis process

184 An ammonia synthesis design is adopted from the paper of Frattini et
 185 al. to replicate the Haber-Bosch Synthesis (HBS) process performance [15].
 186 In the first stage of modeling the ammonia process, the block specifications
 187 provided by the paper are implemented in Aspen Plus[®] (Figure 2) [15]. In
 188 the subsequent step, we simplified the Haber-Bosch synthesis loop to reduce
 189 the computational cost while creating a single link between the generated
 190 wind power and the performance of the HBS process. This model reduc-

191 tion enabled us to govern the process by a single control parameter. To
192 reach this necessary simplification, several adaptations were applied to the
193 HBS loop of Frattini et al. [15]. Frattini et al. originally integrated pressure
194 losses through the use of the tube-and-shell designs in the integrated heat ex-
195 changers (Preheater and Heater in Figure 2) [15]. These pressure losses were
196 discarded from the model, so the reactor compressor which compensated for
197 these pressure losses could therefore be excluded from the model. This model
198 reduction results in the exclusion of the energy consumption of the ammonia
199 synthesis loop. A second modification on the adopted model is the removal of
200 the conditioning block, where water particles from the air or the electrolyzer
201 are cleansed from the flow entering the synthesis loop (Figure 2). Because of
202 the absence of water in both flows, we excluded this condition block from the
203 model. We considered as well pure hydrogen and nitrogen flow rates from the
204 AWE and PSA processes to avoid dealing with the catalyst poisoning caused
205 by the presence of oxygen in both streams, which is a well-reported problem
206 for iron-based catalysts [32]. In industrial processes, a purity of 99.9999%
207 is required with the help of additional purification system to overcome the
208 deactivation of the ammonia synthesis catalyst [32].

209 These modifications resulted in the use of a single control parameter,
210 namely the direct control over the operational pressure within the synthesis
211 loop through the loop compressor. This loop compressor is sequentially gov-
212 erned by the power supply to this component, as is expressed with Equation
213 7 for a three stage compressor.

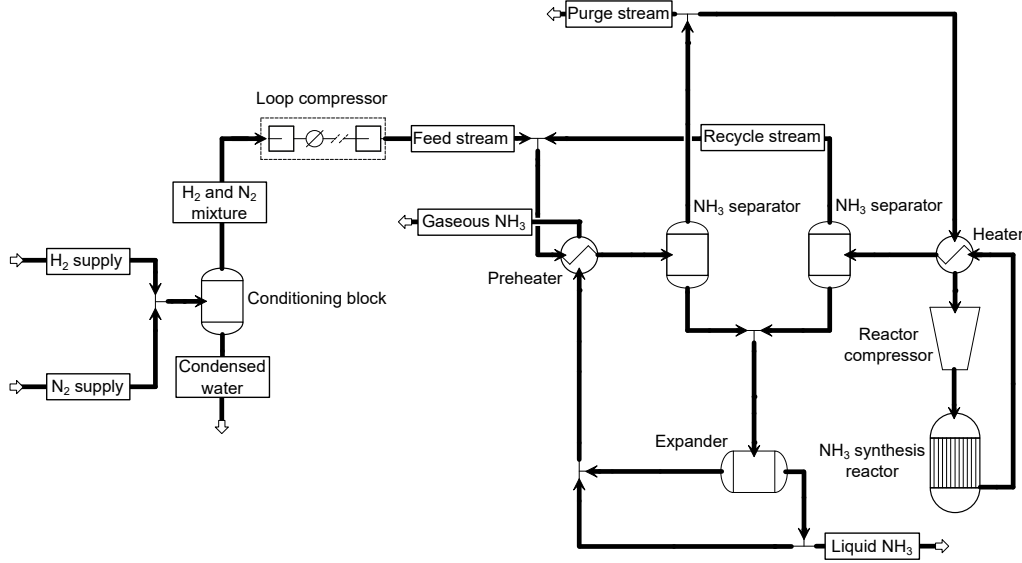


Figure 2: Frattini et al. modeled the Haber-Bosch Synthesis (HBS) loop in Aspen Plus® [15]. In this HBS, the loop compressor pressurizes a mixture of H_2 and N_2 to a certain pressure, where the NH_3 synthesis reactor converts this mixture to NH_3 . The ammonia is extracted from the loop through condensation (NH_3 separators).

$$P_{\text{HBS}} = \frac{\dot{m}_{\text{mix}}}{\eta_{is}\eta_{\text{mech}}} \sum_{i=0}^2 \left(\left(\frac{k}{k-1} \right) T_{i} R \left[\left[\frac{p_{i+1}}{p_i} \right]^{\frac{(k-1)}{k}} - 1 \right] \right) \quad [\text{W}] \quad (7)$$

214 In this expression, P_{HBS} presents the delivered power to Haber-Bosch
 215 compressor in W, \dot{m}_{mix} the mass flow of gas mixture in kg/s, η_{is} isentropic
 216 efficiency, η_{mech} the mechanical efficiency, $T_{\text{in},i}$ inlet temperature of stage i
 217 in K (for $i = 0$ to 2), R the gas constant of mixture in J/kgK, k the heat
 218 capacity ratio, $p_{\text{in},i}$ the inlet pressure in kPa at stage i in kPa (for $i = 0$ to
 219 2) and $p_{\text{out},i+1}$ the outlet pressure in kPa at stage i in kPa (for $i = 0$ to 2).
 220 Frattini et al. provided the design variables of the loop compressor, which
 221 is modeled with a MCompr block in Aspen Plus based on the isentropic

222 compressor model [15]. We compared the HBS power consumption of this
223 simplified process to the reported ammonia synthesis loop in the study of
224 Morgan [33]. This comparison revealed that we obtained very similar results
225 when comparing the relative power consumption in regards to the total power
226 consumption (5.49% with Morgan and 4.44% for our HBS loop). This similar
227 result proves that the applied simplifications is in agreement with another
228 reported PtA energy model.

229 Operational uncertainties and instability phenomenon in the ammonia
230 synthesis process are described in the literature [17, 34], therefore, distur-
231 bances are inherently present in this part of the energy storage model. The
232 paper of Reese et al. acknowledged the presence of uncertainties in practice
233 for a wind-powered ammonia synthesis plant [17]. Although the plant in-
234 tegrated a control system to govern the operations, the measurements of a
235 three-day operation of this plant showed temperature and pressure fluctua-
236 tions during the steady-state process. The paper interpreted this variability
237 due to the undamped nitrogen supply of the PSA system and the occasional
238 absence of hydrogen coming from the electrolysis process. However, these
239 reported temperature fluctuations are essentially present during the opera-
240 tions and reach up to 50°C [17] without a proper identification or analysis
241 of disturbance. The mathematical model of an ammonia synthesis reactor
242 and a heat exchanger of Jinasena et al. showed also temperature oscillations
243 of this process where a temperature fluctuation of 10°C is present [34]. We
244 included the same reactor temperature fluctuation of $\pm 10^\circ\text{C}$ with a Gaussian
245 distribution within this proposed energy storage model. This uncertainty is
246 set into the operational temperature of the REACTOR block of the Aspen

247 Plus model. Although pressure fluctuations were also reported in [17], these
248 variations manifested due to erratic flow supply of hydrogen and nitrogen to-
249 wards the synthesis process, where the origins of the temperature variations
250 were unsubstantiated.

251 **3. Optimization methodology**

252 In this section, the optimization objectives are defined and discussed. The
253 following two subsections designates the design search space and constraints
254 to locate the global optimum within the model constraints. The final part of
255 this section describes the applied MOGA to find these global optimum and
256 the chosen UQ analysis which collectively create the RDO approach. This
257 approach is deemed necessary to maximize the performance of the plant
258 while minimizing the sensitivity of the noise factors on this performance, i.e.,
259 robustifying the wind powered ammonia synthesis process.

260 *3.1. Optimization objective*

261 The optimization objectives of this paper were chosen in function of
262 the considered approach (deterministic or robust design optimization). In
263 the Deterministic Design Optimization (DDO) process, the search algorithm
264 maximizes the storage of wind energy in ammonia while conceiving a design
265 able to continuously operate, i.e. maximizing the plants load factor, which
266 provides a higher energy efficiency and ultimately achieve a better economical
267 return on investment [35]. This load factor (L_F), chosen as the second objec-
268 tive, is expressed by the ratio of average consumed power over time (P_{average})
269 and the plants maximum consumed power ($P_{\text{plant,max}}$) and expressed with
270 Equation 8:

$$L_F = \frac{\sum_{i=1}^t P_{\text{plant}}(i)}{P_{\text{plant,max}}t} = \frac{P_{\text{average}}}{P_{\text{plant,max}}} \quad [-], \quad (8)$$

271 where P_{plant} is the power consumed by the total plant at a certain time in W
 272 and t the time in hours.

273 In the robust design optimization, the robustification of the ammonia
 274 production is opted as the final objective to make it less sensitive to the noise
 275 propagation incorporated in the subsystems. We focused on this objective to
 276 provide a design which is able to capture the highest amount of wind energy
 277 and store it through the production of the studied energy vector while being
 278 less influenced by operational uncertainties. This objective is split in two
 279 parts, where the average ammonia production needs to be maximized and,
 280 secondly, the sensitivity on the ammonia production is minimized. The ratio
 281 of the standards deviation (σ) over its average value (μ) of the concerned
 282 output characterizes this sensitivity, which is defined in literature as the
 283 Coefficient of Variance (CoV). This CoV is expressed in Equation 9 when
 284 applied on the ammonia production:

$$\text{CoV} = \frac{\sigma_{\text{NH}_3}}{\mu_{\text{NH}_3}} \quad [-]. \quad (9)$$

285 3.2. Design search space

286 The optimization method enhances the energy storage model according
 287 to a wind speed data set while finding the best performing plant design
 288 corresponding to the chosen objectives. This best performing design can be
 289 reached by searching the best set of design parameters within the defined
 290 search space. For attaining this best set, specific design parameters were

291 selected to optimize the flow of power to each subsystem (AWE, PSA and
292 HBS).

293 To control the amount of energy captured and converted by the ammonia
294 plant, the simulation disposes of a part of the generated wind power by means
295 of peak shaving; taking the total plant power size as the first design param-
296 eter. This captured power is then subdivided into three fractions, where a
297 proportion of power is supplied to the AWE, another part to the PSA and
298 the residual power to the Haber-Bosch compressor to pressurize the ammo-
299 nia synthesis process. To define the necessary design parameters and attain
300 an optimal configuration among these powers, each of these corresponding
301 subsystems generates hydrogen, nitrogen, and ammonia each at a certain
302 rate. The power sizing of the AWE and PSA are therefore considered as
303 the two successive design parameters, while the power supplied to the HBS
304 compressor is employed as a control parameter (Figure 3). However, a single
305 electrolytic cell can consume a maximum power of 2.1 kW [30], so the stack
306 sizing of the electrolyzer has to be taken into account as well. The number of
307 electrolyzers (N) is therefore selected as the fourth and final design param-
308 eter. The candidates generated by the optimization algorithm for this design
309 parameter are rounded up to the nearest integer.

310 The design search space bounds each design parameter by a minimum
311 and maximum value, so an optimal set of design parameters can be located.
312 For the plant sizing ($\%_{\text{plantsize}}$), the proportion of power flowing to the total
313 ammonia plant can range between 0.001% and 100% according to the 3 MW
314 power capacity of the WTG. This range allows the algorithm to decide which
315 quantity of wind power can be captured by the ammonia plant. The bound-

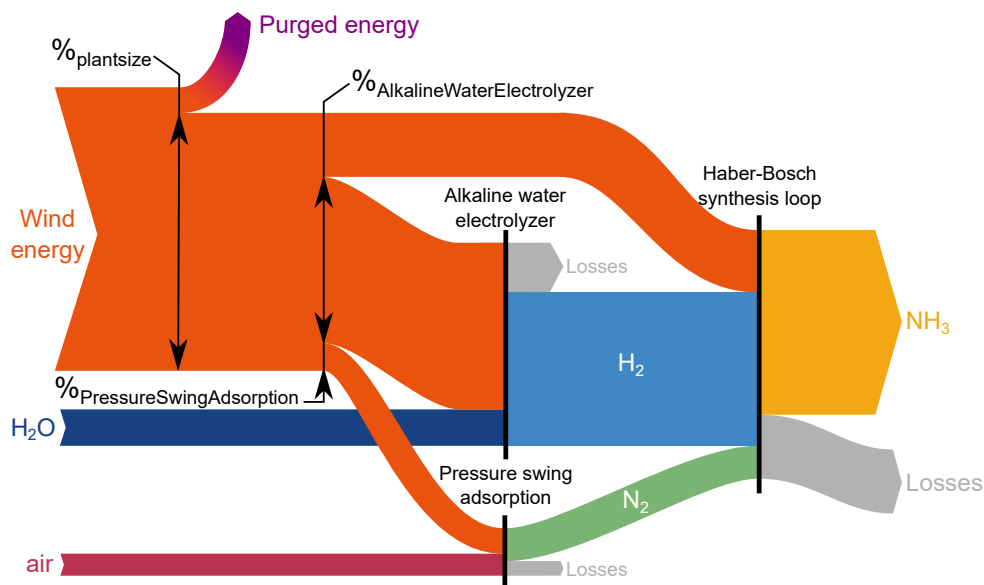


Figure 3: The wind turbine transforms the wind speed into electric power which is then supplied according to a certain ratio to the Alkaline Water Electrolyzer, the Pressure Swing Adsorption and the Haber-Bosch synthesis loop. These processes produce respectively hydrogen, nitrogen and, finally, ammonia through the modeled systems in Aspen Plus. The power ratio towards the individual processes, the plant load size and the numbers of electrolyzers are design parameters defined by the optimization algorithm.

316 aries of the power proportion of the AWE and PSA ($\%_{AWE}$ and $\%_{PSA}$) are
 317 selected based on a sensitivity analysis of the Aspen Plus model. The analy-
 318 sis shows that the proportion of power to the AWE varies between 91% and
 319 95% at optimal/stoichiometric conditions (HBS loop pressure of 250 bar and
 320 a H_2/N_2 ratio of 3 mol/mol). For the PSA, this parameter varies between
 321 0.9% and 1.6%. We chose a range of 1 and 2600 electrolytic cells to assure
 322 the ability of the AWE to perform at an operational power of 3 MW.

323 *3.3. Constraints*

324 Based on the declared restraints by the manufacturer of the alkaline elec-
325 trolyzer and safety regulations of the ammonia synthesis loop, we constrained
326 three output parameters of the total energy storage model. These three pa-
327 rameters are the current density of the electrolytic cell, the H₂/N₂ ratio
328 entering the HBS compressor and its outlet pressure.

329 Each electrolytic cell is bounded by a maximum current density of 300
330 mA/cm² [30]. The minimum current density depends on the thermal effi-
331 ciency (η_{thermal}) which is expressed by Equation 10:

$$\eta_{\text{thermal}} = \frac{U_{\text{tn}}}{U_{\text{real}}} \quad [-] \quad (10)$$

332 where U_{tn} is the thermoneutral voltage in V [30].

333 When the thermal efficiency of the electrolytic cell is higher than 100%,
334 the system requires heat to operate. Because the AWE is a low-temperature
335 electrolyzer, the cell is unable to operate at this point; leading to the elimi-
336 nation of these design parameters from the set of solutions (Figure 4).

337 The flow towards the Haber-Bosch compressor should consist of a H₂/N₂
338 ratio between 2 and 3 [33, 36] while the operating pressure lies between 100
339 and 250 bar [37] (Figure 5). When either of the three output parameters
340 of the model exceeds a limit, the to-be maximized objectives are penalized
341 with a numerical value of 10⁻⁹ and the minimized outputs (the CoV in the
342 RDO phase) with 10⁹. Assigning these numerical values drives the genetic
343 algorithm away from the generated design points and uses the more potent
344 sets of design parameters to evolve towards the best results.

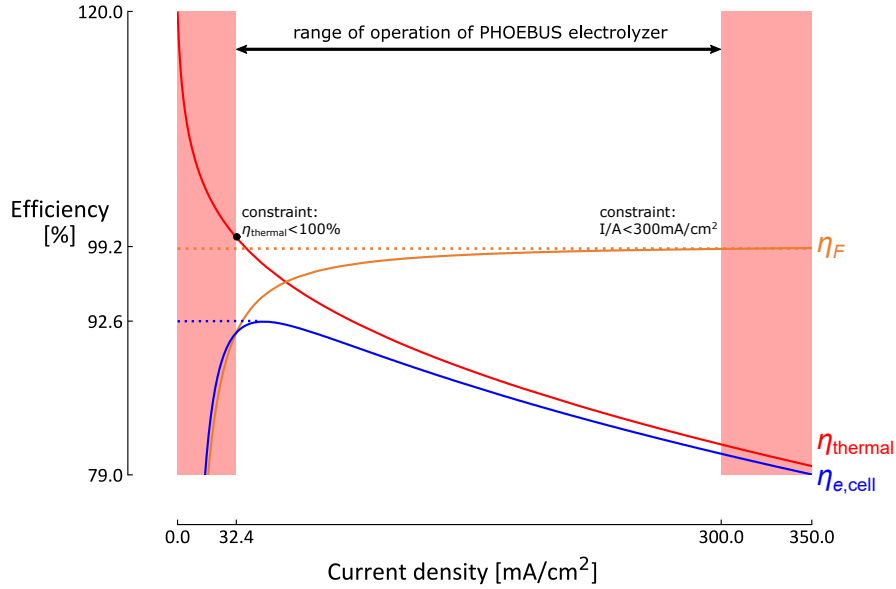


Figure 4: Thermal (η_{thermal}), Faraday (η_F) and energy ($\eta_{e,\text{cell}} = \eta_{\text{thermal}}\eta_F$) efficiency of the alkaline electrolyzer in function of the current density at a temperature of 80°C. A peak in the energy efficiency indicates the most optimal point of operation for the electrolyzer to produce H_2 (related to the Faraday efficiency) while a small amount of losses occur (related to the thermal efficiency). The operational range of the electrolyzer is bounded by a minimum and maximum current density.

345 3.4. Optimization algorithm

346 To determine the optimal set of design samples for the system model, we
 347 implemented the multi-objective Nondominated Sorting Genetic Algorithm
 348 (NSGA-II) [21]. First, the algorithm produces an initial set of design samples
 349 (n samples) through Latin Hypercube Sampling [38]. Out of this initial de-
 350 sign sample set, the algorithm creates a second sample set based on crossover
 351 and mutation, with an equal number of samples n . After characterizing both
 352 sets of design samples, each design sample is implemented in the system
 353 model and evaluated, leading to $2n$ values for each objective. Thereafter,

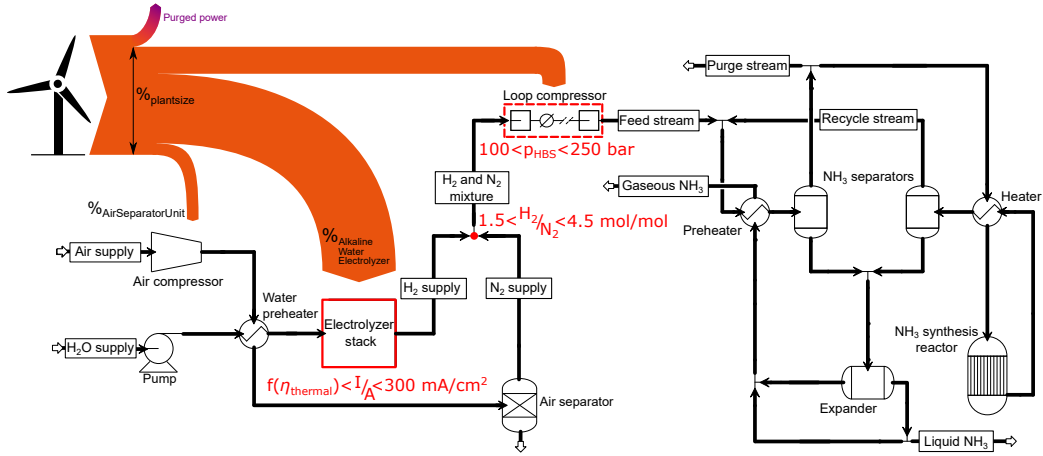


Figure 5: After the optimization algorithm defines the design parameters, a model simulation is executed. A constraint check is then performed to determine if the suggested design is possible without exceeding the minimum and maximum current density of the individual alkaline electrolytic cell, the H_2/N_2 ratio and the output pressure of the Haber-Bosch loop compressor.

354 the samples are sorted based on their dominance on the objectives and the n
 355 samples with the highest dominance define the second generation of design
 356 samples. This iterative process is repeated until a predetermined number
 357 of generations is achieved or the simulation converged towards a solution.
 358 Depending on the relation between the multiple objectives, the optimal set
 359 of design samples can converge to a single optimal design sample (i.e. non-
 360 conflicting objectives) or a set of design samples (i.e. conflicting objectives).
 361 In such a set of optimal design samples, each sample dominates every other
 362 sample in at least one objective (i.e. Pareto frontier).

363 *3.5. Uncertainty quantification method*

364 To propagate the uncertainties of the input parameters through the sys-
365 tem model, we implemented the Polynomial Chaos Expansion (PCE) algo-
366 rithm [39, 40]. This technique provides a computationally efficient alterna-
367 tive for the robust Monte Carlo Simulation technique for a small stochastic
368 dimension (< 10). To quantify the mean and standard deviation of the ob-
369 jective efficiently, the PCE algorithm creates a surrogate model $\hat{M}(\boldsymbol{\xi})$ of the
370 physical model $M(\boldsymbol{\xi})$ based on multivariate orthogonal polynomials Ψ_i and
371 corresponding coefficients u_i :

$$\hat{M}(\boldsymbol{\xi}) = \sum_{i=0}^P u_i \Psi_i(\boldsymbol{\xi}) \approx M(\boldsymbol{\xi}). \quad (11)$$

372 When P in Equation 11 is infinite, the surrogate model is an exact repre-
373 sentation of the physical model. In practice, the series is truncated up to a
374 value depending on the complexity of the input-output relation (related to
375 the polynomial order p) and the stochastic dimension d [22]:

$$P + 1 = \frac{(p + d)!}{p!d!}. \quad (12)$$

376 When the PCE surrogate model is constructed, the mean μ and standard
377 deviation σ follow analytically out of the coefficients:

$$\mu = u_0, \quad (13)$$

$$\sigma = \sum_{i=1}^P u_i. \quad (14)$$

378 Next to the statistical moments of the objective, the contribution of each
 379 input parameter to the objective variation can be quantified through Sobol'
 380 indices. The first-order Sobol' indices (i.e. no input parameter interaction
 381 considered) are defined as:

$$S_i = \frac{D_i}{D} = \frac{\text{Var}[M(\xi_i)]}{\text{Var}[M(\boldsymbol{\xi})]}. \quad (15)$$

382 Similar to the mean and standard deviation, these first-order Sobol' in-
 383 dices can be quantified analytically via the PCE coefficients:

$$S_i^{PC} = \sum_{\alpha \in A_i} u_\alpha / D \quad A_i = \alpha \in A : \alpha_i = 0, \alpha_{j \neq i} = 0. \quad (16)$$

384 4. Results and discussion

385 This section presents the results and discussion of the DDO and RDO ap-
 386 proaches, applied to the power-to-ammonia energy storage system. A global
 387 sensitivity analysis applied on the DDO results shows the effect of the un-
 388 certainties on the performance of two deterministic optimums. To minimize
 389 the effect of the uncertainties on the performance, the RDO approach takes
 390 them into account and find a design that can minimize their effects on these
 391 results. Again, a global sensitivity analysis is performed on the most relevant
 392 designs to show which uncertainties have the most impact on the robustified
 393 designs. Finally, we proposed different measures to further reduce the effect
 394 of these uncertainties on the RDO results.

395 *4.1. Deterministic design optimization*

396 The deterministic design optimization resulted in a collection of optimal
397 solutions when maximizing the annual NH_3 production and the plants load
398 factor. The NSGA-II algorithm obtained this set of solutions –or Pareto
399 points– due to the conflicting objectives: maximizing $m_{\text{NH}_3,\text{total}}$ and L_F .
400 This Pareto front consists of two designs, each configured with two unique
401 design parameters, which enables the optimal performance for a particular
402 objective (Table 2). These two extreme cases are named ‘Most NH_3 ’ and
403 ‘Best L_F ’. Each intermediate set of design parameters between those ex-
404 tremities provides a combination of maximizing both output objectives with
405 a certain weight. The results of the UQ analysis on the two cases show
406 the dominance of the wind speed measurement and the ammonia reactor
407 temperature (Figure 6).

408 The ‘Most NH_3 ’ design enables the highest storage of available wind en-
409 ergy to the energy carrier, ammonia. To obtain this most productive plant,
410 a plant with a load of 2.77 MW (92.4% of the 3 MW WTG capacity) needs
411 to be built while composed of an electrolyzer stack of 2500 individual elec-
412 trolytic cells. This last design parameter (the number of alkaline electrolytic
413 cells) prevents the plant to capture the total wind turbine capacity of 3 MW.
414 When a larger plant size is generated by the genetic algorithm and the same
415 number of electrolyzers is incorporated, the plant would be unable to operate
416 at lower wind power due to the minimum current density (Figure 4). This
417 set of design parameters would result in a lower annual ammonia production
418 and therefore withdrawn from the set of optimal design parameters. The
419 plant comprises of a load factor of 22.4%, which results by definition in a low

Table 2: Set of design parameters and results of the two extremities (‘Most NH₃’ and ‘Best L_F ’) from the Pareto front. An increase in the NH₃ plant size ($\%NH_3size$) increases the amount of electrolyzers (N) and the power distribution to the AWE section ($\%_{AWE}$). This small increase in the power distribution of the AWE relates to the non-linear behavior of the electrolyzer model at a larger power scale.

Design parameter		Case	
		Most NH ₃	Best L_F
$\%_{plantsize}$	[%]	92.4	6.58
N	[-]	2500	954
$\%_{AWE}$	[%]	91.8	91.6
$\%_{PSA}$	[%]	1.60	1.60
Result			
$m_{NH_3,total}$	[tonne]	491	122
L_F	[%]	22.4	73.5

420 utilization rate of the total plant, but for this design case, there is a potential
421 to produce large amounts of ammonia that vary instantaneously with the
422 wind speed. This would be an ideal way to capture the excessive power from
423 the WTG. However, a commercial ammonia synthesis design is not adapted
424 to this flexible functioning [9]. The observed pressure variations are prob-
425 lematic knowing that the ramp-up of the process is time limited (multiple
426 hours to ramp-up the ammonia production) [41]. This could although be
427 solved by accumulating hydrogen and nitrogen gas in storage tanks before
428 the synthesis loop while supplying a constant mass flow of the mixture to
429 the Haber-Bosch process. This makes the system less vulnerable to pressure
430 changes if small fluctuations of power is guaranteed to this part of the plant.

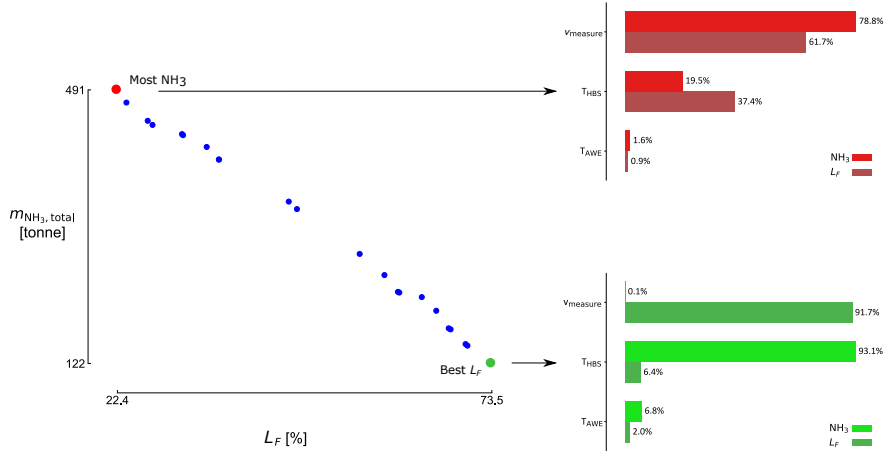


Figure 6: Maximizing the annual NH_3 production and the load factor (L_F) are conflicting objectives. One design can produce 491 tonne of NH_3 but has an L_F of 22.4% while another design produces 122 tonne of NH_3 with an L_F of 73.5%. The UQ analysis of the three operational uncertainties show, through the Sobol' indices, the dominance of the wind speed measurement (v_{measure}) influencing the load factor and the ammonia production in the 'Most NH_3 ' design. The reactor temperature (T_{HBS}) dominates the best L_F design in the ammonia production

431 For the design with the highest load factor ($L_F = 73.5\%$), the plant
 432 consumes 6.58% of the 3 MW WTG capacity (0.197 MW) while consisting
 433 of 954 electrolytic cells. A sensitivity analysis of this design showed that
 434 the NSGA-II algorithm established a plant design with a stable ammonia
 435 production and an electrolyzer stack performing at peak energy efficiency
 436 of 92.6% (Figure 4). This 'Best L_F ' design produces a steady low flow of
 437 ammonia which is almost invulnerable to the variations of wind speed. This
 438 design type is the most common way to produce ammonia in combination
 439 with a grid connection to compensate for the absence of wind power [37], like
 440 the pilot plant in Minnesota [17]. Aside the stable production, the amount

441 of potential wind power discarded from the simulation (73.4% of the residual
442 wind power) is unwanted when the principal use is equalizing the supply and
443 demand of the electric grid. Complementary to the Haber-Bosch plant, the
444 consumption of this residual excess energy in this case provides the necessity
445 to install other flexible storage systems.

446 A global sensitivity analysis showed the effect of uncertainties applied
447 on the two extreme cases together with the corresponding Sobol' indices
448 (Figure 6). The UQ analysis provided a mean value for both objectives
449 which was lower than their deterministic counterparts due to the adverse
450 effect of the uncertainties on the total performance. The analysis applied
451 on the 'Most NH₃' design resulted in a relative decrease of 0.62% in the
452 ammonia production ($\mu_{\text{NH}_3, \text{total}} = 488$ tonne NH₃) and a relative decrease
453 in load factor by 6.63% ($\mu_{L_F} = 20.9\%$). The CoV of the NH₃ production
454 and the load factor of the plant for the 'Most NH₃' case are respectively
455 1.57% and 7.46%. This result subsequently indicates that the load factor
456 of this design is more affected by the variations of the uncertain parameters
457 than the ammonia production. The UQ analysis of the 'Best L_F ' design
458 case presented a relative decrease of 0.56% in NH₃ production and 0.03% for
459 L_F between the mean and the deterministic result, where the CoV of both
460 outcomes in this case are respectively 0.70% and 0.07%. These values show
461 that the deterministic design parameters for the best load factor design from
462 the DDO analysis provides an ammonia plant that is insensitive to variations
463 to the chosen uncertain parameters.

464 Regarding the Sobol' indices, the global sensitivity analysis shows the
465 noise propagation due to the temperature variations in the NH₃ reactor and

466 the electrolytic cell, and the wind speed measurement error in the two cases
467 for each objective (Figure 6). The temperature variations of the electrolyzer
468 have in general less effect on the overall variance of the results (maximum
469 6.8% of the total variance in the ‘Best L_F ’ design).

470 Different operational uncertainties influences the ammonia production in
471 the two extreme cases. In the ‘Most NH_3 ’ case, the wind speed measurement
472 error has a larger effect on the noise propagation of the NH_3 production
473 (78.8%) than in the ‘Best L_F ’ case (0.1%). The influence arises from the
474 fact that the wind speed affects the generated power of the WTG, hence the
475 consumed power by the ammonia plant; making the total NH_3 production
476 more dependable on the wind speed. However in the ‘Best L_F ’ case, the
477 reactor temperature variations dominates the ammonia production (93.1%),
478 while this uncertainty influences in the other case the result with only 19.5%
479 of the total variance. This variation impacts the NH_3 production because
480 of its effect on the equilibrium conditions in the ammonia reactor; directly
481 controlling the amount of ammonia that is produced. The absence of the
482 wind speed measurement error results from the objective to attain a high load
483 factor, which ensures the continuous power flow to the plant; consequently
484 minimizing the effect of the wind speed variation on the NH_3 production.

485 In the case of the load factor, the global sensitivity analysis shows that
486 the wind speed variation has the largest contributions in both cases. This
487 equivalent influence emerges with the definition of the load factor as our
488 second optimization objective (Equation 8).

489 *4.2. Robust design optimization*

490 In the interest to find a design that enables the storage of wind power by
 491 the production of ammonia while minimizing the impact of the uncertainties
 492 on this production, a Robust Design Optimization (RDO) was performed
 493 on the model. Combining the NSGA-II algorithm and the PCE method
 494 provides a strategy to inexpensively measure the sensitivity of the outcome
 495 –or CoV– and progress towards a better set of design parameters, acquired
 496 by the genetic algorithm [40, 42, 43]. This approach optimized the wind-
 497 powered ammonia synthesis model to determine a design which maximizes
 498 the ammonia production while minimizing the CoV of this production.

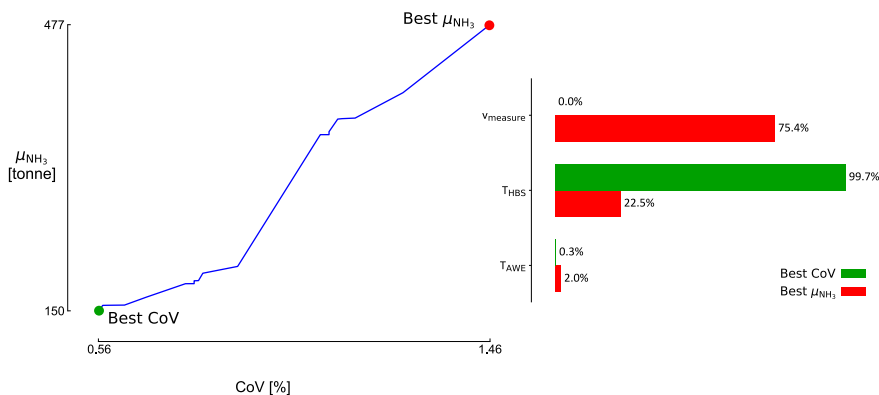


Figure 7: Maximizing the average NH_3 production and minimizing the Coefficient of Variance (CoV) are conflicting objectives. One design can produce 477 tonne of NH_3 but has a CoV of 1.46% while another design produces 150 tonne of NH_3 with a CoV of 0.56%. The NH_3 production of both RDO designs are influenced by the temperature variation of the ammonia reactor. In the ‘Best CoV’ case this variation dominates this result while the ‘Best μ_{NH_3} ’ design is dominated by the wind speed variations.

499 Similar to DDO results, the RDO algorithm provided a trade-off between

500 the two chosen objectives, where two extremities each secure a unique set
501 of design parameters to reach a specific objective (Figure 7). In the most
502 robust case ('Best CoV'), the energy storage system produces on average low
503 quantities of ammonia (150 tonne of NH_3 annually) but consists of a CoV
504 which is 2.6 times lower than the conflicting optimal design. This conflicting
505 case ('Best μ_{NH_3} ') delivers a 3.18 times higher mean production (477 tonne
506 of NH_3 on average) than the 'Best CoV' design. These two opposing designs
507 have a key design parameter which determines this difference in production,
508 namely the fraction of power allowed from the 3 MW wind turbine (i.e.
509 the power plant size). This crucial design parameter creates this trade-off
510 of robustification (Table 3). In comparison with the obtained DDO design
511 parameters (Table 2), the RDO design parameters have a similar design
512 configuration with the 'Most NH_3 ' case of the DDO process. This shows
513 that the exploration and exploitation of the Latin Hypercube and NSGA-
514 II algorithm reaches the same results for the same objective in the different
515 optimization cases. The Gaussian uncertainties causes the different ammonia
516 productions.

517 A global sensitivity analysis of the NH_3 production applied on the two ex-
518 treme trade-off designs resulted in the individual variance of each operational
519 uncertainty presented through the Sobol' indices (Figure 7). According to
520 these Sobol' indices, a different operational uncertainty influences the ammo-
521 nia production of the two designs. In the 'Best CoV' (most robust) design
522 case, the temperature variations of the ammonia reactor dominates this re-
523 sults. If the objective is to create a robust ammonia plant, the temperature
524 variations of the reactor needs to be smaller. Jinasena et al. already pro-

Table 3: Set of design parameters and results of the two extremities (‘Best μ_{NH_3} ’ and ‘Best CoV’) from the Pareto front established by the RDO process. The NH_3 plant size ($\%_{\text{plantsize}}$) is the key design parameter for composing a robust ammonia plant.

Design parameter		Case	
		Best μ_{NH_3}	Best CoV
$\%_{\text{plantsize}}$	[%]	85.7	11.4
N	[-]	2490	2339
$\%_{\text{AWE}}$	[%]	91.9	92.5
$\%_{\text{PSA}}$	[%]	1.59	1.23
Result			
μ_{NH_3}	[tonne]	477	150
CoV	[%]	1.46	0.56

525 vided examples on how to stabilize temperature fluctuations by increasing
 526 the monitoring measurements of the heat exchanger that controls the incom-
 527 ing flow. These measurements consisted of analyzing the composition of feed
 528 gases, feed flow rate, reactor inlet temperature and the pressure along the
 529 reactor [34].

530 In the other case (‘Best μ_{NH_3} ’), a plant design is obtained with a CoV
 531 of 1.46% and an annual ammonia production of 477 tonne which is mostly
 532 influenced by the wind speed measurement error and (in smaller quantities)
 533 the temperature of the HBS reactor. The impact of the accuracy of the
 534 wind speed can be reduced by implementing a more accurate wind speed
 535 measurement device and a better calibration/positioning of the anemometer.

536 As in the deterministic optimization, the temperature variations of the
 537 AWE have little effect on the performance of the ammonia plant although

538 91.9% of the consumed power goes to the alkaline electrolyzer for the pro-
539 duction of H₂.

540 **5. Conclusion**

541 This paper provided the steady-state modeling and optimization of an
542 NH₃-based energy storage system in Aspen Plus[®] based on the expected
543 wind power production from a designed WTG in Python. The integrated
544 WTG powered the AWE, PSA and HBS compressor in a certain ratio, so the
545 storage of wind energy through ammonia production could be optimized by
546 the applied multi-objective optimization approach, i.e. the NSGA-II algo-
547 rithm. Adjacent to the modeling of these subsystems, we identified and inte-
548 grated the wind speed measurement error, the temperature variation of the
549 electrolyzer and the NH₃ synthesis reactor as the operational uncertainties.
550 The PCE algorithm measured the uncertainty propagation of these opera-
551 tional uncertainties when analyzing a certain objective. The multi-objective
552 DDO consisted of maximizing the ammonia production and the plants load
553 factor with the NSGA-II algorithm. In the RDO step, the optimization and
554 robustification of this ammonia production was requested from the NSGA-II
555 algorithm in combination with the PCE method.

556 The DDO step provided a Pareto front where its outer ends delivered a
557 productive and high load factor design. The key difference between these two
558 designs to allow the capture of the wind energy and the continuous operation
559 of the system, arises from two design variables; the sizing of the total storage
560 system and the number of electrolytic cells. A global sensitivity analysis
561 on each objective showed that the temperature variations of the ammonia

562 reactor and the wind speed measurement influences the load factor, while
563 the NH_3 production is either dominated by the wind speed measurement
564 or by the temperature fluctuation in the ammonia reactor. The integrated
565 temperature variations in the AWE has little influence on the noise on each
566 DDO objective.

567 Similar to the DDO case, the robust optimization procedure delivered a
568 trade-off between a productive and a robust design. The key design param-
569 eter for obtaining either one of the two designs lies within the sizing of the
570 total storage system. A larger sized storage system grants the opportunity
571 to produce higher amounts of ammonia but is subjected to the uncertainty
572 of the wind speed measurement and the temperature fluctuation in the am-
573 monia reactor. In contrast to this productive design, the most robust design
574 provides annually lower quantities of ammonia, but is only subjected to the
575 temperature fluctuation of the ammonia reactor and in smaller proportion to
576 the temperature variation in the AWE. Implementing a more accurate wind
577 speed measurement device and increasing the monitoring measurements of
578 the heat exchanger that controls the incoming flow towards the HBS reac-
579 tor can decrease the CoV on the NH_3 production in both RDO cases. A
580 future investigation will involve analyzing the dynamical operations of the
581 power-to-ammonia pathway and robustifying its levelized cost.

582 **Acknowledgments**

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585 licenses.

586 **Appendix A. Parameters alkaline water electrolyzer**

Table A.4: Model parameters of the AWE located in the PHOEBUS plant operating at a pressure of 7 bar and a temperature between 30 and 80°C [30].

U-I design parameters		Value
r_1	$[\Omega\text{m}^2]$	7.33110^{-5}
r_2	$[\Omega\text{m}^2 \text{ }^\circ\text{C}^{-1}]$	-1.1010^{-7}
s_1	$[\text{V}]$	1.58610^{-1}
s_2	$[\text{V } ^\circ\text{C}^{-1}]$	1.37810^{-3}
s_3	$[\text{V } ^\circ\text{C}^{-2}]$	-1.60610^{-5}
t_1	$[\text{m}^2\text{A}^{-1}]$	1.59910^{-2}
t_2	$[\text{m}^2\text{A}^{-1} \text{ }^\circ\text{C}^{-1}]$	-1.302
t_3	$[\text{m}^2\text{A}^{-1} \text{ }^\circ\text{C}^{-2}]$	421.310^2
A	$[\text{m}^2]$	0.25
η_F design parameters		
f_1	$[\%]$	99.5
f_2	$[\text{m}^2\text{A}^{-1}]$	-9.5788
f_3	$[\text{m}^2\text{A}^{-1} \text{ }^\circ\text{C}^{-1}]$	-0.0555
f_4	$[\text{m}^4\text{A}^{-1}]$	1502.7083
f_5	$[\text{m}^4\text{A}^{-1} \text{ }^\circ\text{C}^{-1}]$	-70.8005

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