"Mathematical Education" in Belgium.

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- Belgium in general
- 2 Education in Belgium
- (3) "Mathematical Education"

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Belgium in general

- Where is it?
- What do you need to know about Belgium?
- Education in Belgium
- "Mathematical Education"

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Belgium in Europe



- Member of EU.
- Time zone: UTC + 2 (in Summer)

Belgium





- Capital: Brussels (Capital of EU)
- Languages: French, Dutch, German
- Motto: "Strength through Unity"
- Anthem: The "Brabançonne"
- Area: 30,528 km²
- Population: 11,000,000 (great density)
- Currency: Euro

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History

- Independence from Netherlands: 1830
- Monarchy (but **no** power):
 - First King: Leopold 1st
 - Now: Albert 2nd (he is the 6th king)
- 2 hard periods: first world war ('14-'18) and second ('40-'45)
- $\bullet\,\rightarrow\,$ thanks to Americans who helped us



What to visit and taste?



- Some cities: Brussels, Bruge, Namur, Antwerpen
- Sea (check up forecast bebore!!!) and lots of forested zone
- Of course: chips, chocolate and beers

Some Belgian known?

Movies: Jean-Claude Van Damme ('60)

• Double impact, full contact, JCVD,...



Comics:

- Hergé (Tintin)
- Peyo (The "Schtroumpfs")
- Morris (Lucky Luke)







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Scientists:

- Georges Lemaitre (1894 \rightarrow 1966, Big Bang theory)
- Ilya Prigogine (1917 \rightarrow 2003, Nobel Prize in chemistry)





Some Belgian known?

Mathematicians:

- Pierre Deligne ('44, Fields Medal in '78)
- Jean Bourgain ('54, Fields Medal in '94)





Some Belgian known in sport?

Cycling: Eddy Merckx ('45)

- 5 "Tour de france" ('69->' 74),
- 5 "giro" and 2 "vuelta",
- One day race: 7 "Milan-San Remo", 3 "Tour des flandres", 5 "Liege-Bastogne-Liege", 3 "Paris-roubaix"
- 2 world championships



Tennis: Kim Clijsters ('83)

• 2 US Open, 2 Masters, 1 Fed Cup, Number one...and a girl of 2!!!

and Justine Hénin ('82)

• 2 US Open, 1 Australian Open, 4 French Open, 2 Masters, Olympic champion, 1 Fed cup, number one.





Some Belgian known in sport?

Soccer: team sport number one ('45)

- Olympic champion in 1920
- Second place at European championship in 1980
- Fourth place at World Cup in 1986
- Fourth place at Olympic Games in 2008



Some Belgian known in sport?

Basketball (man): Didier Mbenga ('80 in Congo)

- First Belgian in NBA
- He's playing for Lakers
- Champion in '09



Belgium in general

2 Education in Belgium

- What about politics?
- elementary School
- Secundary School
- Ø High School and Universities

"Mathematical Education"

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 - **Government** (head: Prime Minister (Yves Leterme)): "build" laws
 - Bicameral Parliament (Senate and Chamber of Representatives elected by Belgian people): vote laws
- **Community** one: Community and Region Governments (and Parliaments) for **each** language
- → Many ministers in each topics
- \rightarrow slow system to solve problems!!!
- Remarks: compulsary voting system and only one round.

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- Tests all the time and final exam every year
- Commun final exam in 6th year
- The level gets down slowly year after year (social reasons)

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• One teacher by topic

Tests all the time and final exam in each topics every year

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- The level gets down fastly (political and social reasons)
- Three "levels": Profesional, Technical and General

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Aim: To work directly at 18.

- Manual jobs: bricklayer, finish carpenter,...
- midwife, nursing auxiliary, help-family,...

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Aim:

- Mix up between theoretical and "manual" courses.
- You work at 19 (with one more year) or go to high school
- You can switch to Profesional level at every moment **but not** to general one.

Possibilities:

• accountant, "social teacher", secretary,...

General "level"

Aim:

- Only theoretical courses
- You can switch to technical or profesional level at every moment.
- After, you must go to high school or University.

Problem if you fail.

The **three first** years are commun at everyone in this "level"

- Languages: french (5*h*/*w*), dutch or english (4*h*/*w*), (Latin or greek (4*h*/*w*))
- "Sciences": math (4h/w), sciences (3h/w)
- Miscellaneous: geography (2h/w), history (2h/w), gym (3h/w)
 Then, you choose options (Math-Sciences, (Math-Latin),
 Sciences-Languages,...)
 - **Commun part**: geography (2h/w), history (2h/w), french (4h/w), gym (3h/w),...
 - **Option**: Math $(4h/w \rightarrow 6 \text{ or } 8h/w, \text{ Sciences } (2h/w \rightarrow 5h/w),$ languages $(6h/w \rightarrow 8h/w)$

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High School (3 years)

- Teacher in pre-school or elementary schools
- Math, french, english,... teacher in secundary schools (3 first years)
- Technician (in computer, electricity,...), nurse,...

University (at least 5 years (3+2)), you can study

- Math, french, latin, languages, physics,...
- Political sciences
- Study to become a lawyer
- Business sciences
- Medical sciences (doctor(7y), dentist(5y), pharmacist(5y),...)
- Engineering

Universitary diploma \rightarrow research, teaching in secundary school, working in private,...

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Education in Belgium

Image: "Mathematical Education"

- Math Program at the secundary school
- What to do to be a Teacher at the secondary school?
- S What about research in mathematics?

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Maths in secundary school...general level

- Three first years:
 - Calculus (fractions, (a + b)(c + d) = ..., (a ± b)² = a² ± 2ab + b², powers, square root,...)
 - Geometry (compute area and volumes, Pythagore, Thales, notion of isometry,...)
- **Year** 4:
 - Functions (notion of domain, application, image, study of classical functions, dilatation of functions,...),
 - Equations
- Year 5 (if 6*h*/*w*):
 - Analysis (sequence, limit, derivative)
 - Inequations
 - Analytical geometry (notion of plane, hyperplane,...)
- Year 6 (if 6*h*/*w*):
 - Analysis (integrals, arcsin and arccos functions)
 - Complex space $\mathbb C$
 - Matrices, Determinant

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- Teacher can **not** ask during homeworks, tests or exams something not done in classroom.
 - \rightarrow Students never think by themselves...big trouble in maths!!!
- Exercices must be given in a "live" context or "games"
 - \rightarrow Technics and "boring" calculus are avoided
 - \rightarrow Students do not control basis calculus as well as before.

Aim: to be teacher in secundary school (3 first year)

- you just learn again the program of secundary school (no more)
- lots of pedagogy lessons and practice in schools

Maths at the University: Masters in math

Aim: to do research, to be a teacher in secundary school or work in private (banks,...)

How is it working?

- Bologna Process defined some rules (signed up in '98, started in '04)
 - 5 years: 3 general (called **bac**) and 2 specialized (called **master**)
 - Exams for each courses must be organized twice a year (end of the semester + September)
 - Only the final exam decid if you fail a course...so, no tests during the semester
- Each year, you must obtain 60% in average and 50% in each course
- Professors organize oral exam or written exam

Remark: Level gets down, students **does not control enough** courses and forget very fastly.

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First year:

- Elementary Mathematics (60*h*): recall of the secundary program
- Analysis (180*h*): limit in ℝ^N, continuity, derivative, Taylor development, differential equation (easy)
- Linear algebra (90*h*)
- Algebra (90*h*): notions of group, annulus, permutations,...
- You choose between computer science and physics lessons

Second year:

- Analysis (140h): Frechet derivative, Hilbert space, topology
- Algebra (60*h*): the goal is the Sylow theorems
- Probabilities (60*h*): introduction
- Logic (60*h*): introduction
- Differential manifold and complex analysis(60*h*): introduction
- You again choose between computer science and physics lessons

Third year:

- Analysis (110h): Lebesgue's integration, functional analysis, Banach spaces (L^p, l^p, ...),
- Algebra (45*h*): the goal is the Galois classification
- Probabilities and statistics (45*h*)
- Logic (45*h*)
- Numerical analysis: rootfinding methods, interpolation, Runge-Kutta,
- You again choose between computer science and physics lessons

At this moment, you need to choose between

- To be a **teacher** in secundary school: pedagogy lessons and practice in schools
- To make a **PhD**: followed by a Professor, theoretical courses, go to seminars,...
- To work in **private**: business lessons, probabilities and practice in some companies

Remark: There is a Master-thesis to make in final year.

Two possibilities

- Grant from FNRS(like NRC): 4 years, related to an adviser
- Assistant (payed by the University): 6 years because you **must** give some lessons related to courses of your adviser

Thanks for your attention

Contact: christopher.grumiau@umons.ac.be

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