

Monte Carlo Simulations of the T_2 relaxation induced by exotic-shaped superparamagnetic nanoparticles

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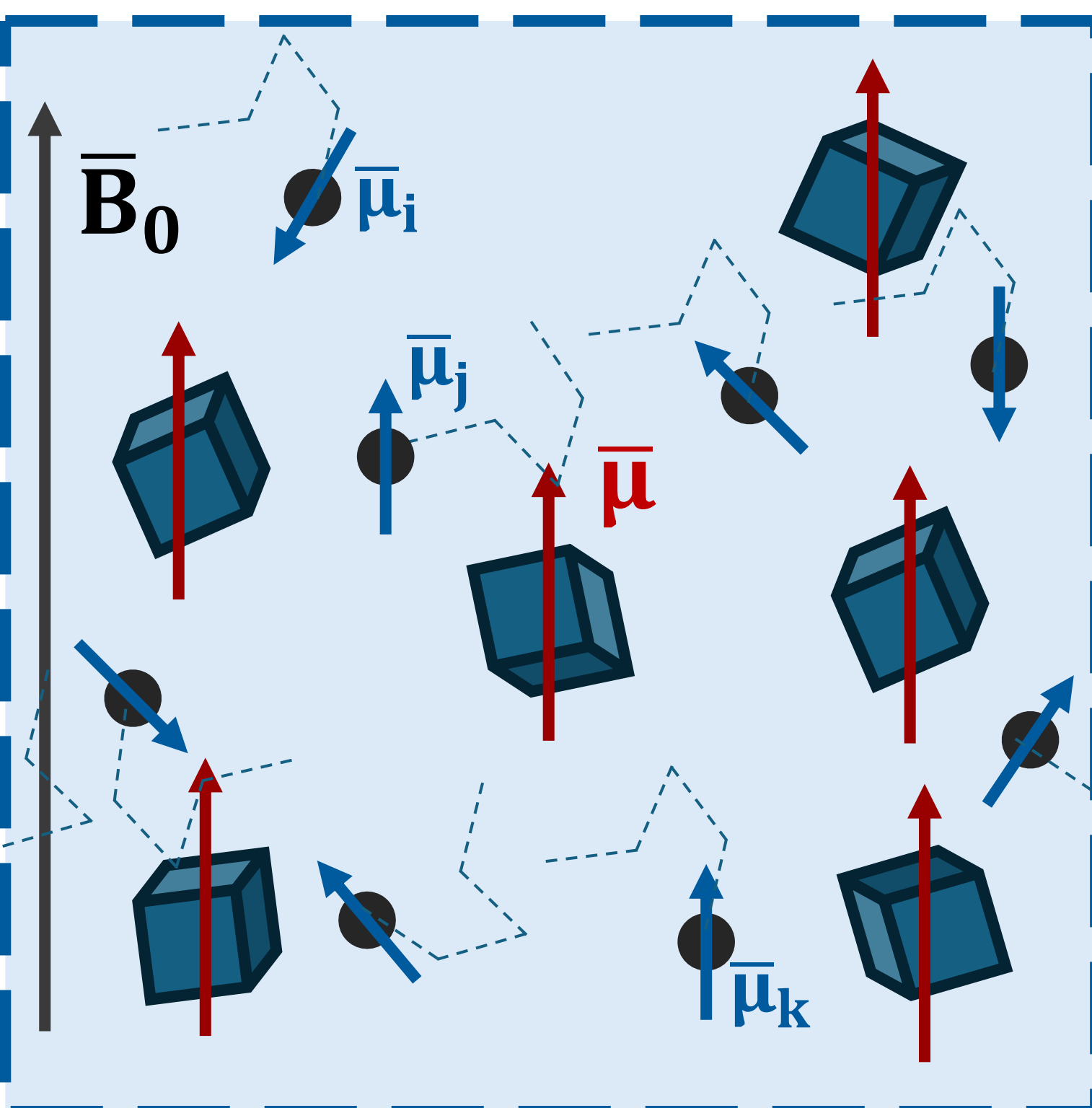
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I. Introduction and research context

The transverse relaxation ($R_2 = 1/T_2$) of water protons induced by *exotic-shaped superparamagnetic nanoparticles* (NPs), used as negative contrast agents in MRI, was studied using **Monte Carlo simulations** under a high static magnetic field (B_0). Comparison with the spherical case, at equal volume, reveals **deviations from the expected relaxation** within the *Motional Average Regime*. **Analytical Stray Field analysis** supports these findings and provides an alternative approach for computing relaxation times of exotic-shaped NPs.

II. Monte Carlo Methodologies

II. a. Diffusion Setup [1]



- 1'500 Magnetite NPs, $\vec{\mu}$
- 10'000 Water Protons, $\vec{\mu}_i$
- Static Magnetic Field \vec{B}_0
- CPMG Sequence ($T_E = 0.25 - 0.5 - 1$ ms)
- Constant volume fraction ($f = 3.14 \cdot 10^{-6} \Leftrightarrow C = 0.211$ mM)
- Periodic Random Walk Diffusion ($D_{\text{water}} = 3 \cdot 10^{-9} \text{ m}^2 \text{ s}^{-1}$)
- Relaxation stems from the **Larmor precession of proton spins** around the **local stray field** (NPs + \vec{B}_0).

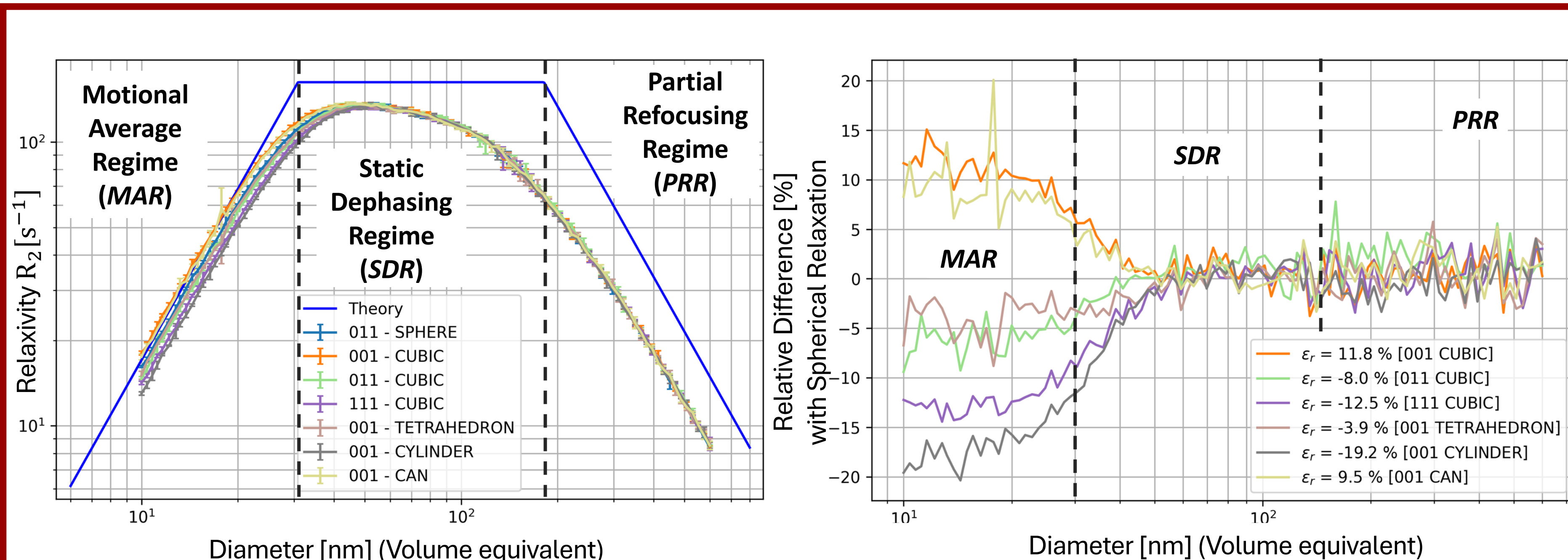
II. b. Stray Field Analysis [2]

- Variation of R_2 induced by NPs at small diameters [3]
 $\Delta R_2 \sim \langle B^2_{\text{proj}} \rangle$
- Extrapolation for other shapes
 $\Delta(\Delta R_2) \sim \Delta(\langle B^2_{\text{proj}} \rangle)$
- Analytical Stray Field derived from scalar potential ϕ_m [4, 5, 6]
 $B(r) = -\mu_0 \nabla \phi_m(r)$
- Using a Monte Carlo Integration,
 $\langle B^2_{\text{proj}} \rangle = \frac{1}{V} \int (B(r \sim U) \cdot \hat{M})^2 dV$

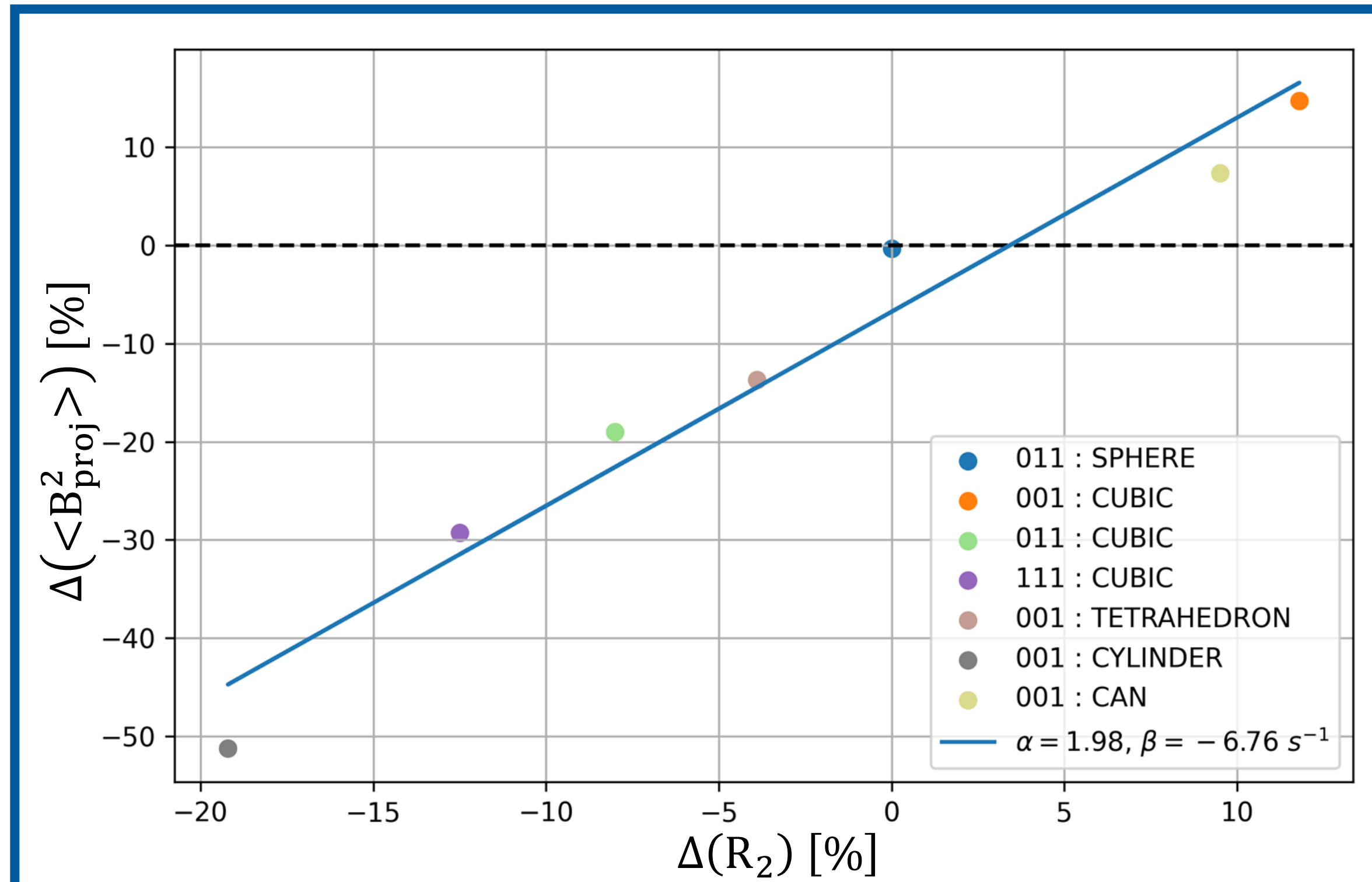
Shape	\hat{M} axis	ϵ_{rel}
Sphere	/	0%
Cubic	111	15%
Cubic	011	-19%
Cubic	001	-29%
Tetrahedron	001	-14%
Cylinder	001	-51%
Can	001	7%

III. Results & Interpretations

III. a. Bell Curves, CPMG at $T_E = 0.5$ ms



III. b. Correlation $\Delta R_2 \sim \langle B^2_{\text{proj}} \rangle$



- Monte Carlo simulations show that significant variations in relaxation times occur at **small NP diameters** (< 40 nm) for all exotic-shaped NP, within the MAR and the lower end of the SDR.
- In addition of particle geometry, we show using cubic-shaped NPs that the **magnetization orientation** can further modulate R_2 , with up to a **25% variation** between 001 and 111 orientations.

- Using the following linear regression :
 $\Delta(\Delta R_2) \approx \alpha \Delta(\langle B^2_{\text{proj}} \rangle) + \beta$
- We propose an **alternative approach to estimate variations in relaxation times** directly from the **stray field variance**, thus **bypassing diffusion simulations**.

IV. Summary And Future Directions

- Monte Carlo diffusion simulations** demonstrate that the **nanoparticle (NP) shape** influences the **transverse relaxation (R_2)** for **small particles (MAR)**, while **larger particles (SDR; and PRR)** remain unaffected.
- By analysing the **analytical stray field** of various particle geometries, we show that **changes in relaxation (ΔR_2)** correlate with **variations in the stray field variance $\langle B^2_{\text{proj}} \rangle$** .
- This suggests that **analytical stray field analysis alone** may be sufficient to **estimate the gain or loss in transverse relaxation time (T_2)** for exotic-shaped nanoparticles within the **MAR**.
- Future work will explore new geometries (e.g., needles, plates, disks) to further **validate the correlation** between ΔR_2 and $\langle B^2_{\text{proj}} \rangle$.

[1] Vuong, Q. L., Gillis, P., Roch, A., & Gossuin, Y. "Magnetic resonance relaxation induced by superparamagnetic particles used as contrast agents in magnetic resonance imaging: a theoretical review". *WIREs Nanomedicine and Nanobiotechnology*, 2017, Vol. 9, Issue 6.
 [2] Fritsche, F., Rosolen, G., De Corte, A., Maes, B., Gossuin, Y., & Vuong, Q. L. (2025). Are nanocubes more efficient than nanospheres to enhance the nuclear magnetic relaxation of water protons? A Monte Carlo simulation study. *The Journal of Chemical Physics*, 162(12).
 [3] Jensen, J. H., & Chandra, R. (2000). NMR relaxation in tissues with weak magnetic inhomogeneities. *Magnetic Resonance in Medicine*, 44(1), 144–156.
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 [5] Nielsen, K. K., Insinga, A. R., & Bjork, R. (2019). The Stray and Demagnetizing Field of a Homogeneously Magnetized Tetrahedron. *IEEE Magnetics Letters*, 10, 1–5.
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